
AP Computer Science A Practice Exam 2

Multiple-Choice Questions

ANSWER SHEET

- 1 (A) (B) (C) (D) (E)
2 (A) (B) (C) (D) (E)
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39 (A) (B) (C) (D) (E)
40 (A) (B) (C) (D) (E)

AP Computer Science A Practice Exam 2

Part I (Multiple Choice)

Time: 90 minutes

Number of questions: 40

Percent of total score: 50

Directions: Choose the best answer for each problem. Use available space for scratch work and hand tracing. Some problems take longer than others. Consider how much time you have left before spending too much time on any one problem.

Notes:

- You may assume all import statements have been included where they are needed.
- You may assume that the parameters in method calls are not null and the methods are called when their preconditions are met.
- You may assume that declarations of variables and methods appear within the context of an enclosing class.
- You may refer to the Java Quick Reference sheet as needed.

1. Consider the following code segment.

```
for (int h = 5; h >= 0; h = h - 2)
{
    for (int k = 0; k < 3; k++)
    {
        if ((h + k) % 2 == 0)
            System.out.print((h + k) + " ");
    }
}
```

What is printed as a result of executing the code segment?

- (A) 5 3 1
- (B) 6 4 2
- (C) 51 31 11
- (D) 6 4 2 0
- (E) 51 31 11 00

2. Consider the following code segment.

```
ArrayList<String> foods = new ArrayList<String>();  
  
foods.add("Hummus");  
foods.add("Soup");  
foods.add("Sushi");  
foods.set(1, "Empanadas");  
foods.add(0, "Salad");  
foods.remove(1);  
foods.add("Curry");  
System.out.println(foods);
```

What is printed as a result of executing the code segment?

- (A) [Salad, Empanadas, Sushi, Curry]
- (B) [Hummus, Salad, Empanadas, Sushi, Curry]
- (C) [Hummus, Soup, Sushi, Empanadas, Salad, Curry]
- (D) [Soup, Empanadas, Sushi, Curry]
- (E) [Hummus, Sushi, Salad, Curry]

3. Consider the following output.

- I.

```
String[] letters = {"A", "P", "C", "S"};
for (int i = letters.length; i > 0; i--)
{
    if (!letters[i].equals("S"))
    {
        for (int k = 0; k < 4; k++)
            System.out.print(letters[k] + " ");
    }
}
```
- II.

```
String letters = "APCS";
for (int i = 0; i < letters.length(); i++)
{
    String s = letters.substring(i, i + 1);
    for (int num = 0; num < 4; num++)
    {
        if (!s.equals("S"))
            System.out.print(s + " ");
    }
}
```
- III.

```
String[][] letters = { {"A", "P"}, {"C", "S"} };
for (String[] row : letters)
{
    for (String letter : row)
    {
        if (!letter.equals("S"))
            System.out.print(letter + " ");
    }
}
```

Which of the following code segments will produce this output?

- (A) I only
- (B) II only
- (C) I and II only
- (D) II and III only
- (E) I, II, and III

Questions 4–5 refer to the following two classes.

```
public class Vehicle
{
    private int fuel;

    public Vehicle(int fuelAmt)
    {
        fuel = fuelAmt;
    }

    public void start()
    {
        System.out.println("Vroom");
    }

    public void changeFuel(int change)
    {
        fuel = fuel + change;
    }

    public int getFuel()
    {
        return fuel;
    }
}
```

```
public class Boat extends Vehicle
{
    public Boat(int fuelAmount)
    {
        super(fuelAmount);
    }

    public void useFuel()
    {
        super.changeFuel(-2);
    }

    public void start()
    {

```

4. Assume the following declaration appears in a client program.

```
super.start();  
Boat yacht = new Boat(20);  
useFuel();  
System.out.println("Remaining Fuel " + getFuel());  
What is printed as a result of executing the call yacht.start()?  
}
```

}

- (A) Vroom
- (B) Remaining Fuel 18
- (C) Remaining Fuel 20
- (D) Vroom
Remaining Fuel 18
- (E) Vroom
Remaining Fuel 20

5. Which of the following statements results in a compile-time error?

- I. Boat sailboat = new Boat(2);
- II. Vehicle tanker = new Boat(20);
- III. Boat tugboat = new Vehicle(10);

- (A) I only
- (B) II only
- (C) III only
- (D) II and III only
- (E) None of these options will result in a compile-time error.

6. Consider the following recursive method.

```
public int weird(int num)  
{  
    if (num <= 0)  
        return num;  
    return weird(num - 2) + weird(num - 1) + weird(num);  
}
```

What value is returned as a result of the call weird(3) ?

- (A) -2
- (B) 3
- (C) 4
- (D) 6
- (E) Nothing is returned. Infinite recursion causes a stack overflow error.

7. Consider the following method.

```
public boolean verifyValues(int[] values)
{
    for (int index = values.length - 1; index > 0; index--)
    {
        /* missing code */
        return false;
    }
    return true;
}
```

The method `verifyValues` is intended to return `true` if the array passed as a parameter is in ascending order (least to greatest), and `false` otherwise.

Which of the following lines of code could replace `/* missing code */` so the method works as intended?

- (A) `if (values[index] <= values[index - 1])`
- (B) `if (values[index + 1] < values[index])`
- (C) `if (values[index] >= values[index - 1])`
- (D) `if (values[index - 1] > values[index])`
- (E) `if (values[index] < values[index + 1])`

8. Consider the following code segment.

```

int[][] matrix = new int[3][3];
int value = 0;

for (int row = 0; row < matrix.length; row++)
{
    for (int column = 0; column < matrix[row].length; column++)
    {
        matrix[row][column] = value;
        value++;
    }
}

int sum = 0;
for (int[] row : matrix)
{
    for (int number : row)
        sum = sum + number;
}

```

What is the value of after the code segment has been executed?

- (A) 0
- (B) 9
- (C) 21
- (D) 36
- (E) 72

9. Consider the following method.

```

public int doStuff(int[] numberArray)
{
    int index = 0;
    int maxCounter = 1;
    int counter = 1;
    for (int k = 1; k < numberArray.length; k++)
    {
        if (numberArray[k] == numberArray[k - 1])
        {
            if (counter <= maxCounter)
            {
                maxCounter = counter;
                index = k;
            }
            counter++;
        }
        else
        {
            counter = 1;
        }
    }
    return numberArray[index];
}

```

Consider the following code segment.

```

int[] intArray = {3, 3, 4, 4, 6};
System.out.println(doStuff(intArray));

```

What is printed as a result of executing the code segment?

- (A) 1
- (B) 3
- (C) 4
- (D) 5
- (E) 6

10. Consider the following code segment.

```
int number = Integer.MAX_VALUE;
while (number > 0)
{
    number = number / 2;
}

for (int i = number; i > 0; i++)
{
    System.out.print(i + " ");
}
```

What is printed as a result of executing the code segment?

- (A) 0
- (B) 1
- (C) 1073741823
- (D) Nothing will be printed. The code segment will terminate without error.
- (E) Nothing will be printed. The first loop is an infinite loop.

11. Consider the following class.

```

public class Automobile
{
    private String make, model;
    public Automobile(String myMake, String myModel)
    {
        make = myMake;
        model = myModel;
    }

    public String getMake()
    { return make; }

    public String getModel()
    { return model; }

    /* Additional implementation not shown */
}

```

Consider the following code segment that appears in another class.

```

Automobile myCar = new Automobile("Ford", "Fusion");
Automobile companyCar = new Automobile("Toyota", "Corolla");
companyCar = myCar;
myCar = new Automobile("Kia", "Spectre");
System.out.println(companyCar.getMake() + " " + myCar.getModel());

```

What is printed as a result of executing the code segment?

- (A) Ford Spectre
- (B) Ford Fusion
- (C) Kia Spectre
- (D) Toyota Corolla
- (E) Toyota Spectre

12. Given the String declaration

```
String course = "AP Computer Science A";
```

What value is returned by the call `course.indexOf("e")`?

- (A) 9
- (B) 10
- (C) 18
- (D) 9, 15, 18
- (E) 10, 16, 19

13. Consider the code segment.

```
if (value == 1)
    count += 1;
else if (value == 2)
    count += 2;
```

Which segment could be used to replace the segment above and work as intended?

- (A)

```
if (value == 1 || value == 2)
    count += 1;
```
- (B)

```
if (value == 1 || value == 2)
    count += 2;
```
- (C)

```
if (value == 1 || value == 2)
    count += value;
```
- (D)

```
if (value == 1 && value == 2)
    count += 1;
```
- (E)

```
if (value == 1 && value == 2)
    count += value;
```

14. A bank will approve a loan for any customer who fulfills one or more of the following requirements:

- Has a credit score ≥ 640
- Has a cosigner for the loan
- Has a credit score ≥ 590 and has collateral

Which of the following methods will properly evaluate the customer's eligibility for a loan?

- I.

```
public boolean canGetLoan(int credit, boolean cosigner, boolean coll)
{
    if (credit >= 640 || cosigner || (credit >= 590 && coll))
        return true;
    return false;
}
```
- II.

```
public boolean canGetloan(int credit, boolean cosigner, boolean coll)
{
    if (!credit >= 640 || !cosigner || !(credit >= 590 && coll))
        return false;
    else
        return true;
}
```
- III.

```
public boolean canGetLoan(int credit, boolean cosigner, boolean coll)
{
    if (coll && credit >= 590)
        return true;
    if (credit >= 640)
        return true;
    if (cosigner)
        return true;
    return false;
}
```

- (A) I only
(B) II only
(C) III only
(D) I and III only
(E) II and III only

15. Consider the following method.

```
public String mixItUp(String entry1, String entry2)
{
    entry2 = entry1;
    entry1 = entry1 + entry2;
    String entry3 = entry1 + entry2;
    return entry3;
}
```

What is returned by the call `mixItUp("AP", "CS")`?

- (A) "APAP"
(B) "APCSAP"

- (C) "APAPAP"
- (D) "APCSCS"
- (E) "APAPAPAP"

16. Assume that `planets` has been a correctly instantiated and initialized array that contains the names of the planets. Which of the following code segments will reverse the order of the elements in `planets`?

- (A)

```
for (int index = planets.length / 2; index >= 0; index--)  
{  
    String temp = planets[index];  
    planets[index] = planets[index + 1];  
    planets[index + 1] = temp;  
}
```
- (B)

```
int index = planets.length / 2;  
while (index >= 0)  
{  
    String s = planets[index];  
    planets[index] = planets[index + 1];  
    index--;  
}
```
- (C)

```
String[] newPlanets = new String[planets.length];  
for (int i = planets.length - 1; i >= 0; i--)  
{  
    newPlanets[i] = planets[i];  
}  
planets = newPlanets;
```
- (D)

```
for (int index = 0; index < planets.length; index++)  
{  
    String temp = planets[index];  
    planets[index] = planets[planets.length - 1 - index];  
    planets[planets.length - 1 - index] = temp;  
}
```
- (E)

```
for (int index = 0; index < planets.length / 2; index++)  
{  
    String temp = planets[index];  
    planets[index] = planets[planets.length - 1 - index];  
    planets[planets.length - 1 - index] = temp;  
}
```

17. Consider the program segment.

```
for (int i = start; i <= stop; i++)  
    System.out.println("AP Computer Science A Rocks!!!");
```

How many times will “AP Computer Science A Rocks!!!” be printed?

- (A) $\text{stop} - \text{start} - 1$
- (B) $\text{stop} - \text{start}$
- (C) $\text{stop} - \text{start} + 1$
- (D) $\text{stop} - 1$
- (E) stop

18. Consider the following code segment.

```
int num = (int) (Math.random() * 30 + 20);  
num += 5;  
num = num / 5;  
System.out.print(num);
```

What are the possible values that could be printed to the console?

- (A) Any real number from 4 to 10 (not including 10)
- (B) Any integer from 5 to 10 (inclusive)
- (C) Any integer from 20 to 49 (inclusive)
- (D) Any integer from 25 to 54 (inclusive)
- (E) Any real number from 30 to 50 (inclusive)

19. Consider the following code segment.

```
String word = "computer";
ArrayList<String> words = new ArrayList<String>();
for (int k = 0; k < word.length(); k++)
{
    words.add(word.substring(k));
    k++;
}

System.out.println(words);
```

What is printed as a result of executing the code segment?

- (A) [computer, mputer, uter, er]
- (B) [computer, comput, comp, co]
- (C) [computer, computer, computer, computer]
- (D) [computer, omputer, mputer, puter, uter, ter, er, r]

20. Consider the following incomplete method.

```
public boolean validation(int x, int y)
{
    /* missing code */
}
```

The following table shows several examples of the desired result of a call to validation.

x	y	Result
1	0	true
3	6	true
1	3	false
2	6	false

Which of the following code segments should replace */* missing code */* to produce the desired return values?

- (A) `return x > y;`
- (B) `return (x % y) > 1`
- (C) `return (x + y) % 2 == 0`
- (D) `return (x + y) % x == y;`
- (E) `return (x + y) % 2 > (y + y) % 2;`

21. Consider the following method that is intended to remove all Strings from words that are less than six letters long. The line numbers are used for reference only.

```
public void letterCountCheck(ArrayList<String> words)
{
Line 1:     int numWord = 0;
Line 2:     while (numWord <= words.size())
            {
Line 3:         if (words.get(numWord).length() < 6)
            {
Line 4:             words.remove(numWord);
            }
            else
            {
Line 5:             numWord++;
            }
        }
    }
```

Which line of code contains an error that prevents letterCountCheck from working as intended?

- (A) Line 1
- (B) Line 2
- (C) Line 3
- (D) Line 4
- (E) Line 5

22. Consider the following recursive method.

```
public void wackyOutput(String wacky)
{
    if (wacky.length() < 1)
        return;
    wacky = wacky.substring(1, wacky.length());
    wackyOutput(wacky);
    System.out.print(wacky);
}
```

What is printed as a result of executing the call
wackyOutput("APCS")?

- (A) PC
- (B) SCPA
- (C) SCSPCS
- (D) PCSCSS
- (E) SCSPCSAPCS

23. Consider the following method.

```
public String calculate(int num1, int num2)
{
    if (num1 >= 0 && num2 >= 0)
        return "Numbers are valid";
    return "Numbers are not valid";
}
```

Which of the following methods will give the exact same results
as calculate?

```
I. public String calculate1(int num1, int num2)
    {
        if (!(num1 < 0 || num2 < 0))
            return "Numbers are valid";
        else
            return "Numbers are not valid";
    }

II. public String calculate2(int num1, int num2)
    {
        if (num1 < 0)
            return "Numbers are not valid";
        if (num2 < 0)
            return "Numbers are not valid";
        else
            return "Numbers are valid";
    }

III. public String calculate3(int num1, int num2)
    {
        if (num1 + num2 < 0)
            return "Numbers are not valid";
        return "Numbers are valid";
    }
```

- (A) I only
- (B) II only
- (C) III only
- (D) I and II only
- (E) I, II, and III

24. Consider the following class declaration.

```
public class TestClass
{
    private double value;

    public TestClass(double value)
    {
        this.value = value;
    }

    public void addValue(double add)
    {
        value += add;
    }

    public void reduceValue(double reduce)
    {
        value -= reduce;
    }

    public double getValue()
    {
        return value;
    }
}
```

The following code segment is executed in the main method.

```
TestClass test1 = new TestClass(9.0);
TestClass test2 = new TestClass(17.5);
test1.reduceValue(3.0);
test2.addValue(1.5);
test2 = test1;
test2.reduceValue(6.0);
System.out.print(test2.getValue() + test1.getValue());
```

What is printed to the console as a result of executing the code segment?

- (A) 0.0
- (B) 3.0
- (C) 12.0
- (D) 19.0
- (E) 27.5

25. Consider the following method.

```
public int guess(int num1, int num2)
{
    if (num1 % num2 == 0)
        return (num2 + num1) / 2;
    return guess(num2, num1 % num2) + (num1 % num2);
}
```

What is the value of `num` after executing the following code statement?

```
int num = guess(3, 17);
```

- (A) 6
- (B) 7
- (C) 10
- (D) Nothing is returned. Modulus by 0 causes an `ArithmeticException`.
- (E) Nothing is returned. Infinite recursion causes a stack overflow error.

26. Consider the following method which implements an Insertion Sort algorithm.

```

public void sortIt(int[] arr)
{
    for (int i = 1; i < arr.length; i++)
    {
        int value = arr[i];
        for (int j = i - 1; j >= 0 && arr[j] > value; j--)
        {
            arr[j + 1] = arr[j];
        }
        arr[j + 1] = value;
    }
}

```

Consider the following array which will be passed to the sortIt method.

```
int[] arr = {4, 3, 7, 6, 1, 5, 2};
```

What does the array contain after the 3rd time through the outer loop ($i == 3$)?

- (A) {4, 3, 7, 6, 1, 5, 2}
- (B) {3, 4, 6, 7, 1, 5, 2}
- (C) {1, 2, 3, 6, 4, 5, 7}
- (D) {1, 2, 3, 4, 7, 6, 5}
- (E) {1, 2, 3, 4, 5, 6, 7}

27. Consider the following class.

```

public class Polygon
{
    /** returns true if the ordered pair is inside the polygon
     *
     *         false otherwise
     */
    // instance variables, constructor, and other methods not shown
}

```

Consider the following class.

```

public class Rectangle extends Polygon
{
    private int topLeftX, topLeftY, bottomRightX, bottomRightY;

    /**
     * Precondition: topLeftX < bottomRightX
     * Precondition: topLeftY < bottomRightY
     * The y value increases as it moves down the screen.
     * @param topLeftX The x value of the top left corner
     * @param topLeftY The y value of the top left corner
     * @param bottomRightX The x value of the bottom right corner
     * @param bottomRightY The y value of the bottom right corner
     */
    public Rectangle(int topLX, int topLY, int bottomRX, int bottomRY)
    {
        topLeftX = topLX;
        topLeftY = topLY;
        bottomRightX = bottomRX;
        bottomRightY = bottomRY;
    }
}

```

Which of the following is a correct implementation of the contains method?

- (A)

```
public boolean contains(int x, int y)
{
    return x > topLeftX && y > topLeftY &&
           x < bottomRightX && y < bottomRightY;
}
```
- (B)

```
public boolean contains(int x, int y)
{
    if (topLeftX > x)
        return true;
    else if (topLeftY > y)
        return true;
    else if (bottomRightX < x)
        return true;
    else if (bottomRightY < y)
        return true;
    return false;
}
```
- (C)

```
public boolean contains(int x, int y)
{ return super.contains(x, y); }
```
- (D)

```
public boolean contains(int x, int y)
{ return Polygon.contains(x, y); }
```
- (E)

```
public boolean contains(int x, int y)
{
    boolean result = false;
    if (topLeftX < x && topLeftY < y)
        result = true;
    if (bottomRightX > x && bottomRightY > y)
        result = true;
    return result;
}
```

28. Consider the following method.

```

public ArrayList<String> rearrange(ArrayList<String> list)
{
    ArrayList<String> myList = list;
    for (int i = myList.size() / 2; i >= 0; i--)
    {
        String wordA = myList.remove(i);
        myList.add(wordA);
    }
    return myList;
}

```

Assume that `ArrayList<String> names` has been correctly instantiated and populated with the following entries.

```
["Nora", "Charles", "Madeline", "Nate", "Silja", "Garrett"]
```

What are the values of the `ArrayList` returned by the call `rearrange(names)`?

- (A) ["Silja", "Garrett", "Nate", "Madeline", "Charles", "Nora"]
- (B) ["Madeline", "Charles", "Nora", "Nate", "Silja", "Garrett"]
- (C) ["Nate", "Silja", "Garrett", "Nora", "Charles", "Madeline"]
- (D) ["Nora", "Charles", "Madeline", "Nate", "Silja", "Garrett"]
- (E) Nothing is returned. `ArrayListIndexOutOfBoundsException`

29. Consider the following code segment.

```

int varA = -30;
int varB = 30;
while (varA != 0 || varB > 0)
{
    varA = varA + 2;
    varB = Math.abs(varA + 2);
    varA++;
    varB = varB - 5;
}
System.out.println(varA + "    " + varB);

```

What will be printed as a result of executing the code segment?

- (A) -30 30
- (B) -4 0
- (C) 0 -4
- (D) 0 4
- (E) -3 -3

30. Consider the following code segment.

```
int[] [] grid = { {0, 1, 2},
                  {3, 4, 5},
                  {6, 7, 8},
                  {9, 10, 11} };

int[] [] newGrid = new int[grid[0].length][grid.length];

for (int row = 0; row < grid.length; row++)
{
    for (int col = 0; col < grid[row].length; col++)
    {
        newGrid[col][row] = grid[row][col];
    }
}
```

What is the value of newGrid[2][1] as a result of executing the code segment?

- (A) 3
- (B) 4
- (C) 5
- (D) 7
- (E) Nothing. There is an ArrayIndexOutOfBoundsException.

31. Consider the following code segment.

```

int[] [] grid = new int[3][3];
for (int row = 0; row < grid.length; row++)
{
    for (int col = 0; col < grid[row].length; col++)
    {
        grid[row][col] = 1;
        grid[col][row] = 2;
        grid[row][row] = 3;
    }
}

```

Which of the following shows the values in grid after executing the code segment?

- (A) { {1, 1, 1},
 {1, 1, 1},
 {1, 1, 1} };
- (B) { {2, 2, 2},
 {2, 2, 2},
 {2, 2, 2} };
- (C) { {3, 2, 2},
 {2, 3, 2},
 {2, 2, 3} };
- (D) { {3, 1, 1},
 {1, 3, 1},
 {1, 1, 3} };
- (E) { {3, 2, 2},
 {1, 3, 2},
 {1, 1, 3} };

32. What can the following method best be described as?

```

public int mystery(int[] array, int a)
{
    for (int i = 0; i < array.length; i++)
    {
        if (array[i] == a)
            return i;
    }
    return -1;
}

```

- (A) Insertion Sort
- (B) Selection Sort
- (C) Binary Search
- (D) Merge Sort
- (E) Sequential Search

33. The following incomplete code is intended to count the number of times the letter key is found in phrase.

```

public static int countOccurrences (String phrase, String key)
{
    int count = 0;
    for (int i = 0; i < phrase.length(); i++)
        /*      missing code      */
    return count;
}

```

Which can be used to replace `/* missing code */` so that `countOccurrences` works as intended?

- (A) `if (phrase == key)`
 `count ++;`
- (B) `if (phrase[i].equals(key))`
 `count ++;`
- (C) `if (phrase.indexOf(i).equals(key))`
 `count ++;`
- (D) `if (phrase.substring(i, i+1) == key)`
 `count ++;`
- (E) `if (phrase.substring(i, i+1).equals(key))`
 `count ++;`

34. Assume `str1` and `str2` are correctly initialized `String` variables. Which statement correctly prints the values of `str1` and `str2` in alphabetical order?

- (A) `if (str1 < str2)`
 `System.out.println(str1 + " " + str2);`
 `else`
 `System.out.println(str2 + " " + str1);`
- (B) `if (str1 > str2)`
 `System.out.println(str1 + " " + str2);`
 `else`
 `System.out.println(str2 + " " + str1);`
- (C) `if (str1.compareTo(str2))`
 `System.out.println(str1 + " " + str2);`
 `else`
 `System.out.println(str2 + " " + str1);`
- (D) `if (str1.compareTo(str2) < 0)`
 `System.out.println(str1 + " " + str2);`
 `else`
 `System.out.println(str2 + " " + str1);`
- (E) `if (str1.compareTo(str2) > 0)`
 `System.out.println(str1 + " " + str2);`
 `else`
 `System.out.println(str2 + " " + str1);`

35. Assume `names` is a `String` array. Which statement correctly chooses a random element from the array?

- (A) `String student = name[(int) (Math.random(names.length))];`
(B) `String student = name[(int) (Math.random(names.length - 1))];`
(C) `String student = name[(int) (Math.random() * names.length) + 1];`
(D) `String student = name[(int) (Math.random() * names.length)];`
(E) `String student = name[(int) (Math.random() * names.length) - 1];`

36. Assume that the variable declarations have been made.

```
int a = 7, b = 15, c = -6;
```

Which will evaluate to true?

- I (a < b) || (b < c)
- II ! (a < b) && (a < c)
- III (a == b) || ! (b == c)

- (A) I only
- (B) II only
- (C) III only
- (D) I and III only
- (E) I, II, and III

Questions 37–38 refer to the following class.

```
public class Coordinates
{
    private int x, y;

    public Coordinates(int myX, int myY)
    {
        x = myX;
        y = myY;
    }

    public void setX(int myX)
    { x = myX; }

    public int getX()
    { return x; }

    public void setY(int myY)
    { y = myY; }

    public int getY()
    { return y; }
}
```

Consider the following code segment.

```
Coordinates c1 = new Coordinates(0, 10);  
Coordinates c3 = c1;  
Coordinates c2 = new Coordinates(20, 30);  
c3.setX(c2.getY());  
c3 = c2;  
c3.setY(c2.getX());  
c2.setX(c1.getX());
```

37. Which of the following calls returns the value 20?

- (A) c1.getX()
- (B) c1.getY()
- (C) c2.getX()
- (D) c2.getY()
- (E) c3.getX()

38. Which of the following calls returns the value 30?

- (A) c1.getX()
- (B) c2.getX()
- (C) c3.getX()
- (D) All of the above
- (E) None of the above

Questions 39–40 refer to the following classes.

Consider the following class declarations.

```

public class Building
{
    private int sqFeet;
    private int numRooms;

    public Building(int ft, int rms)
    {
        sqFeet = ft;
        numRooms = rms;
    }

    public int getSqfeet()
    {
        return sqFeet;
    }

    public String getSize()
    {
        return numRooms + " rooms and " + sqFeet + " square feet";
    }

    /* Additional implementation not shown */
}

public class House extends Building
{
    private int numBedRooms;
    public House(int ft, int rms, int bedrms)
    {
        super(ft, rms);
        numBedRooms = bedrms;
    }

    public String getSize()
    {
        return super.getSqFeet() + " square feet and " + numBedRooms + " bedrooms.";
    }
}

```

39. Assume that `ArrayList<Building> list` has been correctly instantiated and populated with *Building* objects.

Which of the following code segments will result in the square feet in each building being printed?

- I.

```
for (int i = 0; i < list.size(); i++)  
    System.out.println(list.getSqFeet(i));
```
- II.

```
for (int i = 0; i < list.size(); i++)  
    System.out.println(list[i].getSqFeet());
```
- III.

```
for (int i = 0; i < list.size(); i++)  
    System.out.println(list.get(i).getSqFeet());
```
- IV.

```
for (Building b : list)  
    System.out.println(list.getSqFeet());
```
- V.

```
for (Building b : list)  
    System.out.println(b.getSqFeet());
```

- (A) I and IV only
- (B) I and V only
- (C) II and IV only
- (D) III and IV only
- (E) III and V only

40. Consider the following code segment.

```
Building b1 = new Building(2000, 3);  
Building b2 = new House(2500, 8, 4);  
Building b3 = b2;  
Building[] buildings = new Building[3];  
buildings[0] = b1;  
buildings[1] = b2;  
buildings[2] = b3;
```

What will be printed by the following code segment?

```
for (int i = 0; i < buildings.length; i++)  
    System.out.println(buildings[i].getSize());
```

- (A) 3 rooms and 2000 square feet
8 rooms and 2500 square feet
8 rooms and 2500 square feet
- (B) 3 rooms and 2000 square feet
2500 square feet and 4 bedrooms
2500 square feet and 4 bedrooms
- (C) 2000 square feet and 3 bedrooms
2500 square feet and 4 bedrooms
2500 square feet and 4 bedrooms
- (D) 3 rooms and 2000 square feet
2500 square feet and 4 bedrooms
3 rooms and 2000 square feet

STOP. End of Part I.

AP Computer Science A Practice Exam 2

Part II (Free Response)

Time: 90 minutes

Number of questions: 4

Percent of total score: 50

Directions: Write all of your code in Java. Show all your work.

Notes:

- You may assume import statements have been included where they are needed.
- You may assume that all preconditions are met when making calls to methods.
- You may assume that all parameters within method calls are not null.
- Be aware that you should, when possible, use methods that are defined in the classes provided as opposed to duplicating them by writing your own code. Doing so you will not receive full credit.
- You may use the Java Quick Reference sheet as needed.

1. In the seventeenth century, Location Numerals were invented as a new way to represent numbers. Location Numerals have a lot in common with the binary number system we use today, except that in Location Numerals, successive letters of the alphabet are used to represent the powers of two, starting with $A = 2^0$ all the way to $Z = 2^{25}$.

To represent a given number as a Location Numeral (LN), the number is expressed as the sum of powers of two with each power of two replaced by its corresponding letter.

$$A = 2^0 \quad B = 2^1 \quad C = 2^2 \quad D = 2^3 \quad E = 2^4 \quad \text{and so on}$$

Let's consider the decimal number 19.

- 19 can be expressed as a sum of powers of 2 like this: $16 + 2 + 1 = 2^4 + 2^1 + 2^0$.
- We can convert 19 to LN notation by choosing the letters that correspond with the powers of 2: EBA.

Here are a few more examples.

Base 10	Sum of Powers	LN
7	$4 + 2 + 1 = 2^2 + 2^1 + 2^0$	CBA
17	$16 + 1 = 2^4 + 2^0$	EA
12	$8 + 4 = 2^3 + 2^2$	DC

A partial LocationNumeral class is shown below.

```
public class LocationNumeral
{
    private String alphabet = "ABCDEFGHIJKLMNOPQRSTUVWXYZ";

    /** Returns the decimal value of a single LN letter
     *
     * @param letter String containing a single LN letter
     * @return the decimal value of that letter
     * Precondition: the parameter contains a single uppercase letter
     */
    public int getLetterValue(String letter)
    {
        /* to be implemented in part (a) */
    }

    /** Returns the decimal value of a Location Numeral
     *
     * @param numeral String representing a Location Numeral
     * @return the decimal value of the Location Numeral.
     * Precondition: The characters in the parameter are
     *                uppercase letters A-Z only.
     */
    public int getDecimalValue(String numeral)
    { /* to be implemented in part (b) */ }

    /** Builds a Location Numeral
     *
     * @param value int representing the LN value
     * @return String which represents the LN
     *
     * Precondition:  $2^0 \leq \text{value} \leq 2^{26}$ 
     * Postcondition: The letters in the returned String are in
     *                reverse alphabetical order
     */
    public String buildLocationNumeral(int value)
    { /* to be implemented in part (c) */ }

    /* Additional instance variables, constructors, and methods not shown */
}
```

(a) Write the method getLetterValue that returns the numerical value of a single LN letter.

The value of each LN letter is equal to 2 raised to the power of the letter's position in the alphabet string.

For example, if passed the letter “E”, the method will return 16, which is 2^4 .

```
/** Returns the decimal value of a single LN letter
 *
 * @param letter String containing a single LN letter
 * @return the decimal value of that letter
 * Precondition: The parameter contains a single uppercase letter
 */
public int getLetterValue(String letter)
```

- (b) Write the method `getDecimalValue` that takes a Location Numeral and returns its decimal value.

For example, if passed the String “ECA”, the method will add the decimal values of E, C, and A and return the result. In this case: $16 + 4 + 1 = 21$.

You may assume that `getLetterValue` works as intended, regardless of what you wrote in part (a).

```
/** Returns the decimal value of a Location Numeral
 *
 * @param numeral String representing a Location Numeral
 * @return the decimal value of the Location Numeral.
 * Precondition: The characters in the parameter are
 *               uppercase letters A-Z only.
 */
public int getDecimalValue(String numeral)
```

- (c) Write the method `buildLocationNumeral` that takes a decimal value and returns the Location Numeral representation of that decimal value.

For example, if passed the value 43, the method will return the String “FDBA”, which represents the sum $32 + 8 + 2 + 1$.

```

/** Builds a Location Numeral
 *
 * @param value int representing the LN value
 * @return String which represents the LN
 *
 * Precondition: 20 ≤ value ≤ 226
 * Postcondition: The letters in the returned String are in
 *                 descending alphabetical order
 */
public String buildLocationNumeral(int value)

```

2. A quadratic function is a polynomial of degree 2, which can be written in the form $y = ax^2 + bx + c$, where a , b , and c represent real numbers and $a \neq 0$. The x -intercepts, or roots, of a quadratic function can be found by using the quadratic formula.

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

The value of the discriminant $b^2 - 4ac$ determines whether the roots are real or non-real (imaginary). If the discriminant > 0 , the function has 2 real roots. If the discriminant $= 0$ the function has 1 real root, and if the discriminant < 0 , it has imaginary (0 real) roots. Examples are shown in the table.

$y = 1x^2 - 25$	100.0	5.0, -5.0
$y = 1.2x^2 + 3.6x + 2.7$	0.0	-1.5
$y = 2x^2 - 4.1x + 5.2$	-24.79	none

Assume that the following code segment appears in a class other than Quadratic. The code segment shows a sample of using the Quadratic class to represent the three equations shown in the table.

```

double discrim, root1, root2;
Quadratic q1 = new Quadratic(1, 0, -25);
discrim = q1.getDiscriminant();      // discrim is assigned 100.0
if (discrim > 0)
{
    root1 = q1.root1();               // root1 is assigned 5.0
    root2 = q1.root2();               // root2 is assigned -5.0
}
else if (discrim == 0)
    root1 = q1.root1();

Quadratic q2 = new Quadratic(1.2, 3.6, 2.7);
discrim = q2.getDiscriminant();      // discrim is assigned 0.0
if (discrim > 0)
{
    root1 = q2.root1();
    root2 = q2.root2();
}
else if (discrim == 0)
    root1 = q2.root1();               // root1 is assigned -1.5

Quadratic q3 = new Quadratic(2, -4.1, 5.2);
discrim = q3.getDiscriminant();      // discrim is assigned -24.79
if (discrim > 0)
{
    root1 = q3.root1();
    root2 = q3.root2();
}
else if (discrim == 0)
    root1 = q3.root1();

```

Write the Quadratic class. Your implementation must include a constructor that has three double parameters that represent a , b , and c , in that order. You may assume that the value of a is not zero. It must also include a method `getDiscriminant` that calculates and returns the value of the discriminant, a method `root1` and a method `root2` that will calculate the possible two roots of the equation. Your class must produce the indicated results when invoked by the code segment given above.

3. A printing factory maintains many printing machines that hold rolls of paper.

```

public class Machine
{
    private PaperRoll paper;

    public Machine(PaperRoll roll)
    {   paper = roll;   }

    public PaperRoll getPaperRoll()
    {   return paper;   }

    /** Returns the current partial roll and replaces it with the new roll.
     *   @param pRoll a new full PaperRoll
     *   @return the old nearly empty PaperRoll
     */
    public PaperRoll replacePaper(PaperRoll pRoll)
    {
        /* to be implemented in part (a) */
    }

    /* Additional implementation not shown */
}

public class PaperRoll
{
    private double meters;

    public PaperRoll()
    {   meters = 1000;   }

    public double getMeters()
    {   return meters;   }

    /* Additional implementation not shown */
}

```

The factory keeps track of its printing machines in array `machines`, and it keeps track of its paper supply in two lists: `newRolls` to hold fresh rolls and `usedRolls` to hold the remnants taken off the machines when they no longer hold enough paper to be usable. At the beginning of the day, `usedRolls` is emptied of all paper remnants and `newRolls` is refilled. When `newRolls` no longer has enough rolls available to refill all the machines, the factory must shut down for the day until its supplies are restocked. At that time, the amount of paper used for the day is calculated.

A partial `PrintingFactory` class is shown below.

```

public class PrintingFactory
{
    // All machines available in the company
    private Machine[] machines;

    // The available full paper rolls (1000 meters each)
    private ArrayList<PaperRoll> newRolls = new ArrayList<PaperRoll>();

    // The used paper roll remnants (less than 4.0 meters each)
    private ArrayList<PaperRoll> usedRolls = new ArrayList<PaperRoll>();

    public PrintingFactory(int numMachines)
    {
        machines = new Machine[numMachines];
    }

    /** Replaces the PaperRoll for any machine that has a
     * PaperRoll with less than 4.0 meters of paper remaining.
     * The used roll is added to usedRolls.
     * A new roll is removed from newRolls.
     * Precondition: newRolls is not empty.
     */
    public void replacePaperRolls(PaperRoll roll)
    {
        /* to be implemented in part (b) */
    }

    /** Returns the total amount of paper that has been used.
     * @return the total amount of paper that has been used from the PaperRolls
     *         in the usedRolls list plus the paper that has
     *         been used from the PaperRolls on the machines.
     */
    public double getPaperUsed()
    {
        /* to be implemented in part (c) */
    }

    /* Additional implementation not shown */
}

```

- (a) Write the `replacePaper` method of the `Machine` class. This method returns the nearly empty `PaperRoll` and replaces it with the `PaperRoll` passed as a parameter.

```

/** Returns the current partial roll and replaces it with the new roll.
 * @param pRoll a new full PaperRoll
 * @return the old nearly empty PaperRoll
 */
public PaperRoll replacePaper(PaperRoll pRoll)

```

- (b) Write the `replacePaperRolls` method of the `PrintingFactory` class.

At the end of each job cycle, each `Machine` object in `machines` is examined to see if its `PaperRoll` needs replacing. A `PaperRoll` is replaced when it has less than 4 meters of paper remaining.

The used roll is added to the `usedRolls` list, while a new roll is removed from the `newRolls` list.

```
/** Replaces the PaperRoll for any machine in array machines that has
 * a PaperRoll with less than 4.0 meters of paper remaining.
 * The used roll is added to usedRolls.
 * A new roll is removed from newRolls.
 */
public void replacePaperRolls()
```

(c) Write the `getPaperUsed` method of the `PrintingFactory` class.

At the end of the day, the factory calculates how much paper has been used by adding up the amount of paper used from all the rolls in the `usedRolls` list and all the rolls still in the machines. A brand-new paper roll has 1000 meters of paper.

Example

The tables below show the status of the factory at the end of the day.

Paper in Machines	
Amount Left	Amount Used
900.0	100.0
250.0	750.0
150.0	850.0

Paper in usedRolls List	
Amount Left	Amount Used
3.5	996.5
2.0	998.0
1.5	998.5
3.0	997.0

Total used: $100.0 + 750.0 + 850.0 + 996.5 + 998.0 + 998.5 + 997.0 = 5690.0$ meters

Complete the method `getPaperUsed`.

```
/** Returns the total amount of paper that has been used.
 * @return the total amount of paper left on the PaperRolls
 *         in the usedRolls list plus the paper that has
 *         been used from the PaperRolls on the machines.
 */
public double getPaperUsed()
```

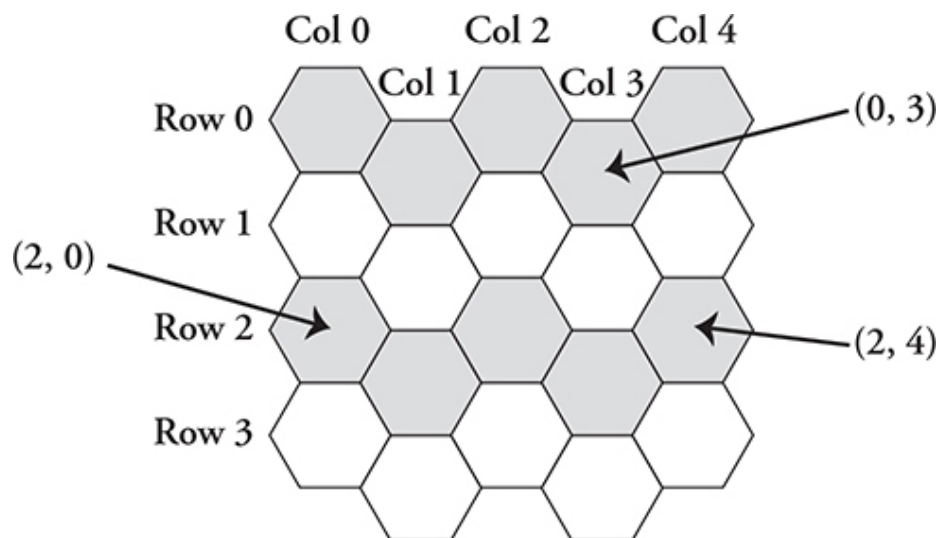
4. A hex grid is a type of two-dimensional (2D) map used by many games to represent the area that tokens, ships, robots, or other types of game pieces can move around on.

The `GamePiece` class is intended to represent the various game pieces required to play different games on the `HexGrid`. The implementation of the `GamePiece` class is not shown. You may construct a `GamePiece` object with a no-argument constructor.

A hex grid is represented in the `HexGrid` class by a 2D array of `GamePiece` objects. The coordinates of a `GamePiece` represent its position on the `HexGrid` as shown in the following diagram. Many of the hex cells in the `HexGrid` will not be occupied by any `GamePiece` and are therefore null.

The rows in a `HexGrid` are in a staggered horizontal pattern where hexes in even columns rise higher than hexes in odd-numbered columns. The columns in a `HexGrid` always appear vertically aligned regardless of the value of the row.

The following is a representation of a `HexGrid` object that contains several `GamePiece` objects at specified locations in the `HexGrid`. The row and column of each `GamePiece` are given.



```

public class HexGrid
{
    /** A two-dimensional array of the GamePiece objects in the
     *   game. Each GamePiece is located in a specific hex cell
     *   as determined by its row and column number.
     */
    private GamePiece[][] grid;

    /** Returns the number of GamePiece objects
     *   currently occupying any hex cell in the grid.
     *
     *   @return the number of GamePiece objects currently in
     *           the grid.
     */
    public int getGamePieceCount()
    { /* to be implemented in part (a) */ }

    /** Returns an ArrayList of the GamePiece objects
     *   in the same column as and with a lower row number than
     *   the GamePiece at the location specified by the parameters.
     *   If there is no GamePiece at the specified location,
     *   the method returns null.
     *
     *   @param row the row of the GamePiece in question
     *   @param column the column of the GamePiece in question
     *   @return an ArrayList of the GamePiece objects "above" the
     *           indicated GamePiece, or null if no such object
     *           exists
     */
    public ArrayList<GamePiece> isAbove(int row, int col)
    { /* to be implemented in part (b) */ }

    /** Adds GamePiece objects randomly to the grid
     *   @ param the number of GamePiece objects to add
     *   @ return true if GamePieces were added successfully
     *           false if there were not enough blank spaces in the
     *           grid to add the requested objects
     */
    public boolean addRandom(int number)
    { /* to be implemented in part (c) */ }

    /* Additional implementation not shown */
}

```

- (a) Write the method `getGamePieceCount`. The method returns the number of `GamePiece` objects in the hex grid.

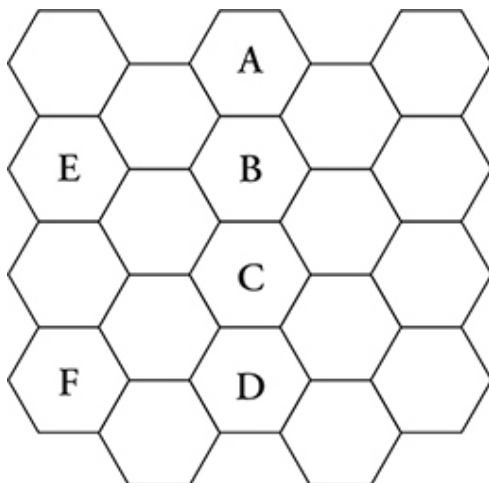
```

/** Returns the number of GamePiece objects
 * currently occupying any hex cell in the grid.
 *
 * @return the number of GamePiece objects currently in
 *         the grid.
 */
public int getGamePieceCount()

```

(b) Write the method `isAbove`. The method returns an `ArrayList` of `GamePiece` objects that are located “above” the `GamePiece` in the row and column specified in the parameters. “Above” is defined as in the same column but with a lower row number than the specified location. In the diagram below, letters represent `GamePiece` objects. The objects may appear in any order in the `ArrayList`.

- If the method is called with the row and column of C, an `ArrayList` containing A and B will be returned.
- If the method is called with the row and column of F, an `ArrayList` containing E will be returned.
- If the method is called with the row and column of E, an empty `ArrayList` is returned.
- If the method is called with the row and column of an empty cell, `null` is returned.



```

/** Returns an ArrayList of the GamePiece objects
 * in the same column as and with a lower row number than
 * the GamePiece at the location specified by the parameters.
 * If there is no GamePiece at the specified location,
 * the method returns null.
 *
 * @param row the row of the GamePiece in question
 * @param column the column of the GamePiece in question
 * @return an ArrayList of the GamePiece objects "above" the
 *         indicated GamePiece, or null if no object exists
 *         at the specified location
 */
public ArrayList<GamePiece> isAbove (int row, int col)

```

- (c) Write the addRandom method. This method takes a parameter that represents the number of GamePiece objects to be added to the grid at random locations. GamePiece objects can only be added to locations that are currently empty (null). If there are insufficient empty cells to complete the requested additions, no GamePiece objects will be added and the method will return false. If the additions are successful, the method will return true.

You may assume that getGamePieceCount works as intended, regardless of what you wrote in part (a). You must use getGamePieceCount appropriately in order to receive full credit for part (c).

```

/** Adds GamePiece objects randomly to the grid
 * @param the number of GamePiece objects to add
 * @return true if GamePieces were added successfully
 *         false if there were not enough empty cells in the
 *         grid to add the requested objects. In this case
 *         no objects will be added.
 */
public boolean addRandom(int number)

```

STOP. End of Part II.

Practice Exam 2 Answers and Explanations

Part I (Multiple Choice)

Answers and Explanations

Bullets mark each step in the process of arriving at the correct solution.

1. The answer is B.

- The outer loop will start at $h = 5$ and then, on successive iterations, $h = 3$ and $h = 1$.
- The inner loop will start at $k = 0$, then 1 and 2.
- The `if` statement will print $h + k$ only if their sum is even (since $\% 2 = 0$ is true only for even numbers).
- Since h is always odd, $h + k$ will be even only when k is also odd. That only happens once per inner loop, when $k = 1$. Adding h and k , we get $5 + 1 = 6$, $3 + 1 = 4$, and $1 + 1 = 2$, so 6 4 2 is printed.

2. The answer is A.

- Let's picture our `ArrayList` as a table. After the first three add statements we have:

Hummus	Soup	Sushi
--------	------	-------

- The `set` statement changes element 1:

Hummus	Empanadas	Sushi
--------	-----------	-------

- Add at index 0 gives us:

Salad	Hummus	Empanadas	Sushi
-------	--------	-----------	-------

- Remove the element at index 1:

Salad	Empanadas	Sushi
-------	-----------	-------

- And finally, add "Curry" to the end of the list:

Salad	Empanadas	Sushi	Curry
-------	-----------	-------	-------

3. The answer is B.

- Option I is incorrect. The outer loop begins at `i = letters.length`. Remember that the elements of an array start at index = 0 and end at index = length - 1. Starting the loop at `i = letters.length` will result in an `ArrayIndexOutOfBoundsException`.
- Option II is correct. The outer loop takes each letter from the string in turn, and the inner loop prints it four times, as long as it is not an "S".
- Option III is incorrect. It correctly traverses each element in the array, but then only prints each element once, not four times.

4. The answer is D.

- The constructor call creates a new `Boat` and the super call sets the fuel variable in the `Vehicle` class to 20.
- The call to the `Boat` class `start` method:
 - begins by calling the `Vehicle` class `start` method, which prints "Vroom",
 - then calls `useFuel`, which calls the `useFuel` method in the `Boat` class, which calls the `Vehicle` class `changeFuel` method, which subtracts 2 from the fuel variable, and
 - finally, the `start` method prints "Remaining Fuel" followed by the value in the `Vehicle` class fuel variable, which is now 18.

5. The answer is C.

- The type on the left side of the assignment statement can be the same type or a super type of the object constructed on the right side of the assignment statement. The object constructed should have an *is-a* relationship with the declared type.
- Option I is correct. A Boat *is-a* Boat.
- Option II is correct. A Boat *is-a* Vehicle.
- Option III is incorrect. Vehicle is a super class of Boat. A Boat *is* a Vehicle, but a Vehicle doesn't have to be a Boat. The super class must be on the left side of the assignment statement.

6. The answer is E.

- This is a recursive method. The first call results in:

$$\text{weird}(3) = \text{weird}(3 - 2) + \text{weird}(3 - 1) + \text{weird}(3)$$

$$= \text{weird}(1) + \text{weird}(2) + \text{weird}(3)$$

A recursive method must approach the base case or it will infinitely recurse (until the Stack overflows). The call to `weird(3)` calls `weird(3)` again, which will call `weird(3)` again, which will call `weird(3)` again....

7. The answer is D.

- It is important to notice that the `for` loop is traversing the array from the greatest index to the least. The array is correct if every element is greater than or equal to the one before it.
- We will return true if we traverse the entire array without finding an exception. If we find an exception, we return false, so we are looking for that exception, or `values[index - 1] > values[index]`.
- Option A is incorrect because of the `=`.
- Note that since we must not use an index that is out of bounds, we can immediately eliminate any answer that accesses `values[index + 1]` which eliminates options B and E.

8. The answer is D.

- The first nested loop initializes all the values in the array in row-major order. The first value entered is 0, then 1, 2, etc. After these loops terminate, the matrix looks like this:

0	1	2
3	4	5
6	7	8

- The second nested loop (for-each loops this time) traverses the array and adds all the values into the sum variable. $0 + 1 + 2 + \dots + 8 = 36$.

9. The answer is C.

- doStuff is going to loop through the array, checking to see if each item is the same as the item before it. If it is, the values of index, maxCounter, and counter all change. If it is not, only counter changes.
- Begin by setting `index = 0`; `maxCounter = 1`; `counter = 1`; and noting that `numberArray.length() = 5`.
- First iteration: `k = 1`, enter the loop with `index = 0`; `maxCounter = 1`; `counter = 1`;
 - Item 1 = item 0, execute the if clause
 - `counter <= maxCounter`, execute the if clause
 - `maxCounter = 1`; `index = 1`
 - `counter = 2`
- Second iteration: `k = 2`, enter the loop with `index = 1`; `maxCounter = 1`; `counter = 2`;
 - Item 2 $\neq$ item 1, execute the else clause
 - `counter = 1`
- Third iteration: `k = 3`, enter the loop with `index = 1`; `maxCounter = 1`; `counter = 1`;
 - Item 3 = item 2, execute the if clause
 - `counter <= maxCounter`, execute the if clause

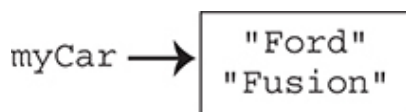
- `maxCounter = 1; index = 3`
- `counter = 2`
- Fourth iteration: `k = 4`, enter the loop with `index = 3`; `maxCounter = 1; counter = 2`;
 - Item 4 `!=` item 3, execute the else clause
 - `counter = 1`
 - Fifth iteration: `k = 5`, which fails the condition and the loop exits.
 - `index = 3`, `numberArray[3] = 4` is returned and printed.

10. The answer D.

- `Integer.MAX_VALUE` is a large number, but repeatedly dividing by 2 will eventually result in an answer of 0 and the loop will terminate. Remember that this is integer division. Each quotient will be truncated to an integer value. There will be no decimal part.
- In the second loop, the initial condition sets `i = 0`, which immediately fails the condition. The loop never executes, so nothing is printed, but the code segment terminates successfully.

11. The answer is A.

- `myCar` is instantiated as a reference variable pointing to an `Automobile` object with instance variables `make = "Ford"` and `model = "Fusion"`.



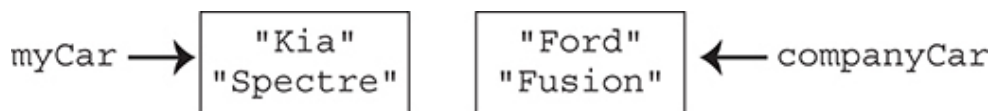
- `companyCar` is instantiated as a reference variable pointing to an `Automobile` object with instance variables `make = "Toyota"` and `model = "Corolla"`.



- The statement `companyCar = myCar` reassigns the `companyCar` reference variable to point to the same object as the `myCar` variable. They are now aliases of each other. The original `companyCar` object is now inaccessible (unless yet another variable we don't know about points to it).



- The next statement instantiates a brand-new `Automobile` object with `make = "Kia"` and `model = "Spectre"`. It sets the `myCar` reference variable to point to this new object. This does not change the `companyCar` variable.
- The `companyCar` variable still points to the object with instance variables `make = "Ford"` and `model = "Fusion"`.



- So we print `companyCar's make`, which is `"Ford"` followed by `myCar's model`, which is `"Spectre"`.

12. The answer is A.

- The `indexOf(str)` method returns the index of the first occurrence or `-1` if not found.
- The index position begins counting at 0. "e" is found at position 9.

13. The answer is C.

- Both of the conditions in the original segment add 1 or 2, which is value, to count.
- The conditions can be combined using an `||` statement.

14. The answer is D.

- Option I is correct. Note that the final condition, `(credit >= 590 && coll)`, doesn't have to be in parentheses. Since AND has a higher priority than OR, it would be executed first, even

without the parentheses. However, the parentheses make the code clearer, and that is always our goal.

- Option II is incorrect. While it seems reasonable at first glance, De Morgan's theorem tells us we can't just distribute the !. We also have to change OR to AND.
- Option III is correct. As soon as a condition evaluates to true, the method will return and no more statements will be executed. Therefore no else clauses are required. The method will return false only if none of the conditions are true.

15. The answer is C.

- To answer this problem, you need to understand that `String` objects are immutable (the only other immutable objects in our Java subset are `Integer` and `Double`).
- When the method begins, `entry1 = "AP"` and `entry2 = "CS"`.
- Then the assignment statement reassigns `entry2` so that both variables now refer to the `String` object containing "AP".
- When we execute the next statement, `entry1 = entry1 + entry2`, we would expect that to change for both variables, since they both reference the same object, but `String` objects don't work that way. Whenever a string is modified, a new `String` object is created to hold the new value. So now, `entry1` references "APAP" but `entry2` still references "AP".
- We put those together, and "APAPAP" is returned.

16. The answer is E.

- Remember, we only need to find one error to eliminate an option.
- Option A is incorrect. `index` starts in the middle of the array and goes down to zero. We swap the item at `index` with the item at `index + 1`. We are never going to address the upper half of the array.
- Option B is incorrect. The swap code is incomplete. We put `planets[index]` into `s`, but then never use `s`.

- Option C is incorrect. It's OK to use another array, but this code forgets to switch the order when it moves the elements into the new array. The new array is identical to the old one.
- Option D is incorrect. At first glance, there's no obvious error. The swap code looks correct. Although `planets.length - 1 - index` seems a bit complex, a few examples will show us that it does, indeed, give the element that should be swapped with the element at index: $0 \rightarrow 7 - 0 = 7$, $1 \rightarrow 7 - 1 = 6$, $2 \rightarrow 7 - 2 = 5$, $3 \rightarrow 7 - 3 = 4$, and so on. The trouble with this option is that "and so on" part. It swaps all the pairs and then continues on to swap them all again. After completing the four swaps listed above, we are done and we should stop.
- Option E is correct. The code is the same as option D, except it stops after swapping half the elements. The other half were the partners in those first swaps, so now everything is where it should be.

17. The answer is C.

- The loop begins at whatever value is stored in `start` and will continue until the value stored in `stop` is reached.
- Try substituting `start = 1` and `stop = 5`. The loop will execute 5 times.
- Substituting 1 and 5 into the answer options, A, B, and D are eliminated.
- Choosing different values for `start` and `stop` such as 2 and 10 will result in option C.

18. The answer is B.

- The general form for generating a random number between *high* and *low* is
`(int)(Math.random() * (high - low + 1)) + low`
- $high - low + 1 = 30$, $low = 20$, so $high = 49$
- After the first statement, `num` is an integer between 20 and 49 (inclusive).

- In the second statement, we add 5 to num. Now num is between 25 and 54 (inclusive).
- In the third statement we divide by 5, remembering integer division. Now num is between 5 and 10 (inclusive).

19. The answer is A.

- This loop takes pieces of the String "computer" and places them in an ArrayList of String objects.
- The loop starts at index $k = 0$, and adds the word.substring(0), or the entire word, to the ArrayList. The first element of the ArrayList is "computer".
- Then k is incremented by the $k++$ inside the loop, $k = 1$, and immediately incremented again by the instruction in the loop header, $k = 2$. It is bad programming style to change a loop index inside the loop, but we need to be able to read code, even if it is poorly written.
- The second iteration of the loop is $k = 2$, and we add word.substring(2) or "mputer" to the ArrayList.
- We increment k twice and add word.substring(4) or "uter".
- We increment k twice and add word.substring(6) or "er".
- We increment k twice and fail the loop condition. The loop terminates and the ArrayList is printed.

20. The answer is E.

- We need to plug the values of x and y into the given statements to see if they always generate the correct return value.
- Option A is incorrect. $3 > 6$ is false, but should be true.
- Option B is incorrect. $1 \% 0$ will fail with a division by zero error.
- Option C is incorrect. $(1 + 0) \% 2 == 0$ is false, but should be true.
- Option D is incorrect. $(3 + 6) \% 3 == 6$ is false, but should be true.
- Option E works for all the given values.

21. The answer is B.

- The loop will continue until `numWord = words.size()`, which will cause an `ArrayIndexOutOfBoundsException`.
- Notice that `numWord` is only incremented if nothing is removed from the `ArrayList`. That is correct because, if something is removed, the indices of the elements after that element will change. If we increment `numWord` each time, we will skip elements.

22. The answer is C.

- This is an especially difficult example of recursion because the recursive call is not the last thing in the method. It's also not the first thing in the method. Notice that the print happens *after* the call. So each iteration of the method will print one letter less than its parameter.
- Let's trace the code. The parts in *italics* were filled in on the way back up. That is, the calls in the plain type were written top to bottom until the base case returned a value. Then the answers were filled in *bottom to top*.

<code>wackyOutput("APCS")</code>	$\rightarrow$ <i>print "PCS"</i>	(printed fourth)
<code>wackyOutput("PCS")</code>	$\rightarrow$ <i>print "CS"</i>	(printed third)
<code>wackyOutput("CS")</code>	$\rightarrow$ <i>print "S"</i>	(printed second)
<code>wackyOutput("S")</code>	$\rightarrow$ <i>print ""</i>	(printed first)
<code>wackyOutput("")</code>	$\rightarrow$ Base Case. Return without printing.	

Remember that the returns are read bottom to top, so the output is "SCSPCS" in that order.

- Note that `"S".substring(1,1)` is not an error. It returns the empty string.

23. The answer is D.

- Option I is correct. It uses De Morgan's theorem to modify the boolean condition.

```
!(num1 >= 0 && num2 >= 0)
!(num1 >= 0 ) || !(num2 >= 0)
num1 < 0 || num2 < 0
```

- Option II is correct. It tests the two parts of the condition separately. If either fails, it returns "Numbers are not valid".
- Option III is incorrect. If num1 is a positive number and num2 is a negative number, but the absolute value of num2 < num1 (num1 = 5 and num2 = -2, for example), option III will return "Numbers are valid" although clearly both numbers are not >= 0.

24. The answer is A.

- test1 references a TestClass object with value = 9.0 and test2 references a TestClass object with value = 17.5.



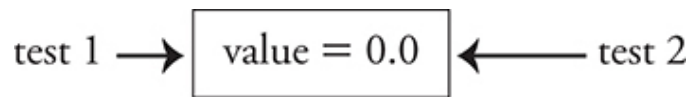
- After the addValue and reduceValue calls, our objects look like this:



- The assignment statement changes test2 to reference the same object as test1.



- At this point, the object with value = 19.0 is inaccessible (unless another reference variable we don't know about is pointing to it). The next time Java does garbage collection, it will be deleted.
- The next reduceValue call changes our object to this:



- The `getValue` statements in the next line get the same value, as `test1` and `test2` are pointing to the same object. $0.0 + 0.0 = 0.0$.

25. The answer is B.

- This is a recursive method. Let's trace the calls. The parts in *italics* were filled in on the way back up. That is, the calls in the plain type were written top to bottom until the base case returned a value. Then the answers were filled in *bottom to top*.
- Be very careful to get the order of `num1` and `num2` correct in the modulus operation and the parameters correct in the recursive call.
 - $\text{guess}(3, 17) = \text{guess}(17, 3) + 3 = 4 + 3 = 7$ which gives us our final answer.
 - $\text{guess}(17, 3) = \text{guess}(3, 2) + 2 = 2 + 2 = 4$
 - $\text{guess}(3, 2) = \text{guess}(2, 1) + 1 = 1 + 1 = 2$
 - $\text{guess}(2, 1)$ Base case! return $3/2 = 1$ (integer division)

26. The answer is B.

This method implements a standard insertion sort. In this sort, each item is taken in turn and placed in its correct position among the items to its left (with lower indices).

- The first time through the loop, $i = 1$, the algorithm looks at the first two values $\{4, 3\}$ and inserts the 3 in the right place $\{3, 4\}$. The rest of the array is untouched.
- The second time through, $i = 2$, the algorithm looks at the first three values $\{3, 4, 7\}$. Since the 7 is already in the right place, no changes are made.
- The third time through, $i = 3$, the algorithm looks at the first four values $\{3, 4, 7, 6\}$ and inserts the 6 in the right place $\{3, 4, 6, 7\}$. Our answer is $\{3, 4, 6, 7, 1, 5, 2\}$.

- If we were to continue, the final three values, $\{...1, 5, 2\}$ would be inserted in their correct locations during the remaining 3 iterations of the outside loop.

Note: Answer C is the result of the third pass of a standard selection sort algorithm.

27. The answer is A.

- In order for a rectangle to contain a point, the following conditions must be true:
 $topLeftX < x < bottomRightX$ and $topLeftY < y < bottomRightY$
- Option A is correct. These are the exact conditions used in option A, though they are in a different order.
- Option B is incorrect because it will return true if any one of the four conditions is true.
- Options C and D are incorrect because they attempt to make invalid calls to `super` or `Polygon` methods that do not exist.
- Option E is incorrect. It is similar to option B, except that it will return true if two of the required conditions are true.

28. The answer is A.

- Let's show the contents of the `ArrayList` graphically and trace the code. The method is called with this `ArrayList`.

Nora	Charles	Madeline	Nate	Silja	Garrett
------	---------	----------	------	-------	---------

- The first time through the loop, $i = 3$. The element at index 3 is removed and added to the end of the `ArrayList`.

Nora	Charles	Madeline	Silja	Garrett	Nate
------	---------	----------	-------	---------	------

- Decrement i , $i = 2$, which is ≥ 0 , so execute the loop again. The element at index 2 is removed and added to the end.

Nora	Charles	Silja	Garrett	Nate	Madeline
------	---------	-------	---------	------	----------

- Decrement i , $i = 1$, which is ≥ 0 , so execute the loop again. The element at index 1 is removed and added to the end.

Nora	Silja	Garrett	Nate	Madeline	Charles
------	-------	---------	------	----------	---------

- Decrement i , $i = 0$, which is ≥ 0 , so execute the loop again. The element at index 0 is removed and added to the end.

Silja	Garrett	Nate	Madeline	Charles	Nora
-------	---------	------	----------	---------	------

- Decrement i , $i = -1$, which fails the loop condition. The loop terminates and the `ArrayList` is returned.

29. The answer is C.

- The loop will execute while $\text{varA} \neq 0$ OR $\text{varB} > 0$. Another way to say that, using De Morgan's theorem, is that the loop will *stop* executing when $\text{varA} == 0$ AND $\text{varB} \leq 0$.
- The only answer that fits that condition is C: $\text{varA} = 0$ and $\text{varB} = -4$.
- Instead of thinking through the logic, we could trace the execution of the loop, but it's a lot of work. Here's a table of the values of varA and varB at the end of every iteration of the loop until the loop terminates.

varA	varB
-27	21
-24	18
-21	15
-18	12
-15	9
-12	6
-9	3
-6	0
-3	-3
0	-4

30. The answer is C.

- The nested loops go through grid in row-major order, but assign into newGrid in column-major order. (Notice that newGrid is instantiated with its number of rows equal to the grid's number of columns and its number of columns equal to the grid's number of rows.) After executing the loops, newGrid looks like this:

```
{ {0, 3, 6, 9 },  
  {1, 4, 7, 10 },  
  {2, 5, 8, 11 } }
```

- newGrid [2][1] = 5

31. The answer is E.

- The nested loops traverse the entire array. Each time through, the three assignment statements are executed. The key to the problem is the order in which these statements are executed. We need to pay attention to which values will overwrite previously assigned values.
- On entering the loops, our array looks like this:

0	0	0
0	0	0
0	0	0

- We will execute the outer loop three times, and for each of those three times, we will execute the inner loop three times.
- The first iteration of both loops, we are changing element [0][0].
 - The first statement makes it a 1.
 - Note that this statement changes the array in row-major order.
 - The second statement makes it a 2.
 - Note that this statement changes the array in column-major order.

- The third statement makes it a 3, so it will remain a 3.
 - Note that this statement only changes the diagonals.
- Completing the first cycle of the inner loop, the first statement assigns a 1 to $[0][1]$ and $[0][2]$ and the second statement assigns a 2 to $[1][0]$ and $[2][0]$. The third statement repeatedly sets $[0][0]$ to 3, and since that statement is last, it will remain a 3.

3	1	1
2	0	0
2	0	0

- The next cycle of the inner loop will assign a 1 to $[1][0]$, $[1][1]$, and $[1][2]$. A 2 will be assigned to $[0][1]$, $[1][1]$, and $[2][1]$. Then element $[1][1]$ will be overwritten with a 3.

3	2	1
1	3	1
2	2	0

- The third (and last) cycle of the inner loop will assign a 1 to $[2][0]$, $[2][1]$, and $[2][2]$. A 2 will be assigned to $[0][2]$, $[1][2]$, and $[2][2]$. Then element $[2][2]$ will be overwritten with a 3.

3	2	2
1	3	2
1	1	3

32. The answer is E.

- If this were a sorting algorithm, there would be only one parameter, the array to be sorted, and a sorted array would be returned, so we can eliminate the sorting algorithms. In addition, Merge Sort is recursive, and selection and insertion

sorts require nested loops, neither of which appear in this code.

- Binary search repeatedly divides the remaining section of the array in half. There's no code that does anything like that. This is not a binary search.
- This code goes through the array one step at a time in order. This is a sequential search algorithm.

33. The answer is E.

- Each pass of the loop needs to check one letter to see if it is the desired key.
- The `substring(i, i+1)` method is used to look at one letter at a time.
- Each time the letter matches the key, then `count` is incremented by 1.

34. The answer is D.

- The `compareTo(other)` method returns 0 if the `string` object is less than other (which means it comes first alphabetically)
- Strings cannot be compared using `==`, `<`, or `>` operators.

35. The answer is D.

- `Math.random()` doesn't take any parameter, so options A and B can be eliminated.
- `Math.random()` returns a value greater than or equal to 0.0 and less than 1.0.
- Once the random `double` is returned, it must be multiplied by the size of the array and then cast into an `integer`.

36. The answer is D.

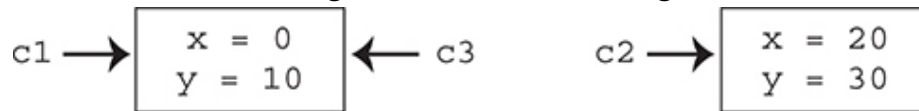
- Only I and III evaluate to true.

37. The answer is D.

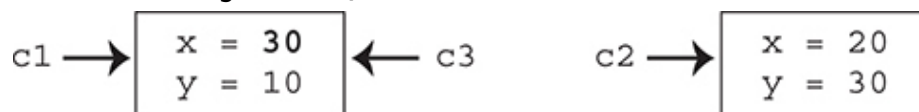
- This question is explained along with question 38.

38. The answer is D.

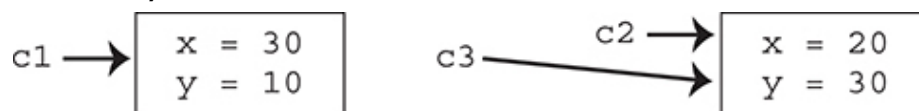
- We will solve questions 37 and 38 together by diagramming the objects and reference variables.
- The first three assignment statements give us:



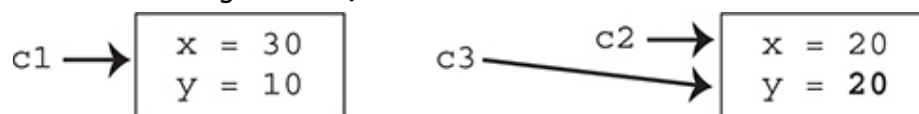
- `c3.setX(c2.getY());` results in:



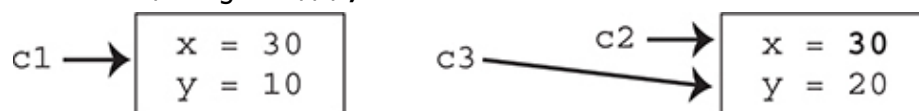
- `c3 = c2;` results in:



- `c3.setY(c2.getX());` results in:



- `c2.setX(c1.getX());` results in:



- Question 37: Both `c2.getY()` and `c3.getY()` return 20, but only `c2.getY()` is an option.
- Question 38: `c1.getX()`, `c2.getX()`, and `c3.getX()` all return 30.

39. The answer is E.

- Option I is incorrect. Among other errors, `getSqFeet` does not take a parameter.
- Option II is incorrect. Square brackets are used to access elements of arrays, but not of `ArrayLists`.
- Option III is correct.

- Option IV is incorrect. list is the name of the ArrayList, not the name being used for each element of the ArrayList.
- Option V is correct.

40. The answer is B.

- The array holds Building objects. As long as an object *is-a* Building, it can go into the array.
- The runtime environment will look at the type of the object and call the version of getSize written specifically for that object.
 - list[0] is a Building so the Building class getSize will be used to generate the String for list[0].
 - list[1] is a House so the House class getSize will be used to generate the String for list[1].
 - list[2] references the same object as list[1]. This will generate a duplicate of the list[1] response.

Part II (Free Response)

Answers and Explanations

Please keep in mind that there are multiple ways to write the solution to a Free-response question, but the general and refined statements of the problem should be pretty much the same for everyone. Look at the algorithms and coded solutions, and determine if yours accomplishes the same task.

General Penalties (assessed only once per problem)

- 1 using local variables without first declaring them
- 1 returning a value from a void method or constructor
- 1 accessing an array or ArrayList incorrectly
- 1 overwriting information passed as a parameter
- 1 including unnecessary code that causes a side effect such as a compile error or console output

1. Location Numerals

- (a) **General Problem:** Write the `getLetterValue` method that returns the numerical value of the given letter.

Refined Problem: Find the parameter letter's position in the `String` `alphabet`. Return 2 raised to that power.

Algorithm:

- Use `indexOf` to find the position of letter in the `String` `alphabet`.
- Use `Math.pow` to raise 2 to the power of the position found.
- Return the result.

Java Code:

```
public int getLetterValue(String letter)
{
    int position = alphabet.indexOf(letter);
    return (int) Math.pow(2, position);
}
```

- (b) **General Problem:** Write the `getDecimalValue` method that takes a Location Numeral and returns its decimal equivalent.

Refined Problem: Find the value of each letter in turn and add it to running total. Return the final answer.

Algorithm:

- Create a variable to hold the running total.
- Loop through the Location Numeral `String` from the letter at index 0 to the end of the `String`.
 - Isolate each letter, using `substring`.
 - Call the method `getLetterValue`, passing the isolated letter.
 - Add the result to the running total.
 - When the loop is complete, return the total.

Java Code:

```

public int getDecimalValue(String numeral)
{
    int total = 0;
    for (int i = 0; i < numeral.length(); i++)
    {
        String letter = numeral.substring(i, i + 1);
        total += getLetterValue(letter);
    }
    return total;
}

```

Common Errors:

- Don't end the loop at `numeral.length() - 1`. When you notice the expression `numeral.substring(i, i + 1)`, you may think that the `i + 1` will cause an out of bounds exception. It would if it were the first parameter in the substring, but remember that the substring will stop *before* the value of the second parameter, so it will not index out of bounds. If you terminate the loop at `numeral.length() - 1`, you will miss the last letter in the String.
- Be sure that you use the method you wrote in part (a). There is generally a penalty for duplication of code if you rewrite the function in another method. The problem usually has a hint when a previously written method is to be used. In this case, the problem says, "You may assume that `getLetterValue` works as intended, regardless of what you wrote in part (a)." That's a surefire indication that you'd better use the method to solve the current problem.

(c) General Problem: Write the `buildLocationNumeral` method that returns the Location Numeral representation of the decimal value passed as a parameter.

Refined Problem: Determine which powers of 2 sum together to give the value of the parameter. Build the Location Numeral by determining the corresponding letters of the alphabet.

Algorithm:

- Initialize a variable to keep track of the position in the alphabet string starting at the end.
- Initialize a string variable to the empty string and add letters as appropriate.
- As long as more simplification can be done:
 - Determine the value of 2^{current} position in alphabet string.
 - If the power of 2 value is larger than the current value variable
 - Concatenate the corresponding alphabetic letter onto the string variable.
 - Decrease the value by the power of 2.
 - Decrease the position variable by 1.
- Return the final result.

Java Code:

```
public String buildLocationNumeral(int value)
{
    int position = 26;
    int powerOf2;
    String temp = "";
    while (value > 0)
    {
        powerOf2 = (int) Math.pow(2, position);
        if (value >= powerOf2)
        {
            temp += alphabet.substring(position, position + 1);
            value -= powerOf2;
        }
        position --;
    }
    return temp;
}
```

Common Errors:

- This is a tricky piece of code. There are many places where errors can sneak in. Remember that you can earn most of the points for a question even with errors or missing sections in your code.

- The key is continuously subtracting powers of 2 from value until value becomes 0 and determining the letter of the alphabet that corresponds to that power of 2.

Scoring Guidelines: Location Numerals

Part (a)	getLetterValue	2 points
+1	Determines the correct position in the alphabet string	
+1	Returns the correct value	
Part (b)	getDecimalValue	3 points
+1	Accesses every individual letter in numeral; no bounds errors, no missing values	
+1	Calls getLetterValue for each letter	
+1	Accumulates and returns the correct total value	
Part (c)	buildLocationNumeral	4 points
+1	Initializes appropriate variables	
+1	Determines the appropriate power of 2 for each time through the loop	
+1	Adds the appropriate letter of the alphabet to the string for each time through the loop	
+1	Returns the accumulated string	

Sample Driver:

There are many ways to write these methods. Maybe yours is a bit different from our sample solutions and you are not sure if it works. Here is a sample driver program. Running it will let you see if your code works and will help you debug it if it does not.

Copy the `LocationNumeralDriver` into your IDE along with the `LocationNumeral` class (including your solutions).

- Here's the `LocationNumeralDriver`:

```

public class LocationNumeralDriver
{
    public static void main(String[] args)
    {
        LocationNumeral num1 = new LocationNumeral();
        System.out.println(num1.getLetterValue("E"));
        System.out.println(num1.getDecimalValue("ECA"));
        System.out.println(num1.buildLocationNumeral(43));

        LocationNumeral num2 = new LocationNumeral();
        System.out.println(num2.getLetterValue("B"));
        System.out.println(num2.getDecimalValue("CBA"));
        System.out.println(num2.buildLocationNumeral(17));
    }
}

```

2. Quadratic

(a) **General Problem:** Write the Quadratic class.

Refined Problem: Create the Quadratic class with three instance variables and one three parameter constructor. The three methods `getDiscriminant`, `getRoot1`, and `getRoot2` will need to be defined.

Algorithm:

- Write a class header for Quadratic.
- Declare three instance variables to store the values of a , b , and c .
- Write a constructor with three parameters that represent the coefficients of the quadratic equation and assign the parameters to the corresponding instance variables.
- Write method `getDiscriminant`.
- Write methods `getRoot1` and `getRoot2`.

Java Code:

```

public class Quadratic
{
    private double a, b, c;

    public Quadratic(double a, double b, double c)
    {
        this.a = a;
        this.b = b;
        this.c = c;
    }

    public double getDiscriminant()
    {
        return b * b - 4 * a * c;
    }

    public int getRoot1()
    {
        return (-b + Math.sqrt(getDiscriminant())) / (2 * a);
    }

    public int getRoot2()
    {
        return (-b - Math.sqrt(getDiscriminant())) / (2 * a);
    }
}

```

Common Errors:

- The instance variables must be declared private.

Scoring Guidelines: Quadratic

Quadratic class		1 point
+1	Complete, correct header for <code>Quadratic</code>	
state maintenance		1 point
+1	Declares at least three private instance variables capable of maintaining the coefficients of the quadratic equation	
Quadratic Constructor		2 points
+1	Correct method header	
+1	Sets appropriate state variables based on parameters	
getDiscriminant		2 points
+1	Correct method header	
+1	Returns the correctly computed value	
getRoot1, getRoot2		3 points
+1	Correct method headers for <code>getRoot1</code> and <code>getRoot2</code>	
+1	Correctly calculates and returns <code>root1</code>	
+1	Correctly calculates and returns <code>root2</code>	

Sample Driver:

There are many ways to write these methods. Maybe yours is a bit different from the sample solutions shown here and you are not sure if it works. Here is a sample driver program. Running it will let you see if your code works, and will help you debug it if it does not.

Copy `QuadraticDriver` into your IDE along with the complete `Quadratic` class (including your solutions). You also might want to add the `toString` method to your `Quadratic` class, which will print the quadratic equation for you.

```
public String toString()
{
    return a + "x^2 + " + b + "x + " + c;
}
```

```

public class QuadraticDriver
{
    public static void main(String[] args)
    {
        Quadratic q1 = new Quadratic(1, 0, -25);
        double discrim = q1.getDiscriminant();
        System.out.println("The quadratic equation " + q1 + " with discriminant " +
            discrim);
        if (discrim > 0)
            System.out.println("has two real roots: " + q1.root1() + " and " +
                q1.root2());
        else if (discrim == 0)
            System.out.println("has one real root: " + q1.root1());
        else
            System.out.println("has no real roots");
        System.out.println();

        Quadratic q2 = new Quadratic(1.2, 3.6, 2.7);
        discrim = q2.getDiscriminant();
        System.out.println("The quadratic equation " + q2 + " with discriminant " +
            discrim);
        if (discrim > 0)
            System.out.println("has two real roots: " + q2.root1() + " and " +
                q2.root2());
        else if (discrim == 0)
            System.out.println("has one real root: " + q2.root1());
        else
            System.out.println("has no real roots");
        System.out.println();

        Quadratic q3 = new Quadratic(2, -4.1, 5.2);
        discrim = q3.getDiscriminant();
        System.out.println("The quadratic equation " + q3 + " with discriminant " +
            discrim);
        if (discrim > 0)
            System.out.println("has two real roots: " + q3.root1() + " and " +
                q3.root2());
        else if (discrim == 0)
            System.out.println("has one real root: " + q3.root1());
        else
            System.out.println("has no real roots");
    }
}

```

3. Printing Factory

- (a) **General Problem:** Write the `replacePaper` method of the `Machine` class.

Refined Problem: Take the new `PaperRoll` passed as a parameter and use it to replace the current roll. Return the used roll to the caller. Notice that this is a type of swapping and will require a temp variable.

Algorithm:

- Create a temp variable of type `PaperRoll`.

- Assign the machine's PaperRoll paper to temp.
- Assign the new PaperRoll passed as a parameter to the machine's PaperRoll.
- Return the PaperRoll in temp.

Java Code:

```
public PaperRoll replacePaper(PaperRoll pRoll)
{
    PaperRoll temp = paper;
    paper = pRoll;
    return temp;
}
```

Common Errors:

- It may seem like you want to do this:

```
return paper;
paper = pRoll;
```

But once the return statement is executed, flow of control passes back to the calling method. The second statement will never be executed.

- (b) **General Problem:** Write the `replacePaperRolls` method of the `PrintingFactory` class.

Refined Problem: Traverse the `machines` `ArrayList` checking for `Machine` object with `PaperRoll` objects that contain less than 4.0 meters of paper. Any `PaperRoll` objects containing less than 4.0 meters of paper need to be replaced. Get a new `PaperRoll` object from the `newRolls` `ArrayList`, and pass it to the `Machine` class `replacePaper` method. Place the returned used `PaperRoll` object on the `usedRolls` `ArrayList`.

Algorithm:

- Write a `for-each` loop to traverse the `machines` array.

- If the current Machine object's PaperRoll object contains < 4.0 m of paper:
 - Take a PaperRoll object off of the newRolls ArrayList.
 - Call replacePaper passing the new roll as a parameter.
 - replacePaper will return the old PaperRoll object; put it on the usedRolls ArrayList.

Java Code:

```
public void replacePaperRolls()
{
    for (Machine m : machines)
    {
        if (m.getPaperRoll().getMeters() < 4.0)
        {
            PaperRoll newRoll = newRolls.remove(0);
            PaperRoll oldRoll = m.replacePaper(newRoll);
            usedRolls.add(oldRoll);
        }
    }
}
```

Common Errors:

- The syntax for accessing the amount of paper remaining is complex, especially when using a for loop instead of a for-each loop. Remember that the getMeters method is not a method of the Machine class. We have to ask each Machine object for access to its PaperRoll object and then ask the PaperRoll object how much paper it has left.

Java Code Alternate Solution #1:

Use for loops instead of for-each loops.

Use just one variable for the old and new rolls.

```

public void replacePaperRolls()
{
    for (int i = 0; i < machines.length; i++)
    {
        if (machines[i].getPaperRoll().getMeters() < 4.0)
        {
            PaperRoll roll = newRolls.remove(0);
            roll = machines[i].replacePaper(roll);
            usedRolls.add(roll);
        }
    }
}

```

Java Code Alternate Solution #2:

Combine the statements and eliminate the variables altogether. This could also be done in the for loop version.

```

public void replacePaperRolls()
{
    for (Machine m : machines)
        if (m.getPaperRoll().getMeters() < 4.0)
            usedRolls.add(m.replacePaper(newRolls.remove(0)));
}

```

(c) **General Problem:** Write the `getPaperUsed` method of the `PrintingFactory` class.

Refined Problem: The amount of paper used on each roll is 1000 minus the amount of paper remaining. First traverse the `usedRolls` `ArrayList` and add up the paper used. Next, traverse the `machines` array and add up the paper used. These two amounts represent the total paper used. Return the sum.

Algorithm:

- Write a for-each loop to traverse the `usedRolls` `ArrayList`.
 - Add 1000 minus paper remaining on the current roll to a running sum.
- Write a for-each loop to traverse the `machines` array.

- Add 1000 minus paper remaining on the current machine's roll to the same running sum.
- Return the sum.

Java Code:

```
public double getPaperUsed()
{
    double sum = 0.0;
    for (PaperRoll p : usedRolls)
        sum = sum + (1000 - p.getMeters());

    for (Machine m : machines)
        sum = sum + (1000 - m.getPaperRoll().getMeters());

    return sum;
}
```

Java Code Alternate Solution #1:

Use for loops instead of for-each loops.

Replace `sum = sum + ...` with `sum += ...`

```
public double getPaperUsed()
{
    double sum = 0.0;
    for (int i = 0; i < usedRolls.size(); i++)
        sum += 1000 - usedRolls.get(i).getMeters();

    for (int i = 0; i < machines.length; i++)
        sum += 1000 - machines[i].getPaperRoll().getMeters();

    return sum;
}
```

Common Errors:

- Remember that ArrayLists and arrays use different syntax both to access elements and to find their total number of elements.

Java Code Alternate Solution #2:

There are other ways to compute the paper use. Here we add up all the leftover paper and then subtract the total from $1000 * \text{the total number of rolls}$. This technique could be combined with the for loop version, as well as the for-each loop as shown here.

```
public double getPaperUsed()
{
    double totalLeft = 0.0;
    double totalUsed = 0.0;

    for (PaperRoll p : usedRolls)
        totalLeft += p.getMeters();

    for (Machine m : machines)
        totalLeft += m.getPaperRoll().getMeters();

    totalUsed = 1000 * (usedRolls.size() + machines.length) - totalLeft;

    return totalUsed;
}
```

Scoring Guidelines: Printing Factory

Part (a) **replacePaper** **2 points**

- +1 Assigns the `PaperRoll` object passed as a parameter to the `Machine` object's `PaperRoll` variable; specifically: `paper = pRoll`;
- +1 Returns the used `PaperRoll` object

Part (b) **replacePaperRolls** **3 points**

- +1 Accesses all elements of `machines`; no bounds errors, no missed elements
- +2 Processes low-paper rolls correctly
 - +1 Removes a new roll from the `newRolls` `ArrayList`; calls the `replacePaper` method; passing the new roll as a parameter
 - +1 Adds the used roll returned from the `replacePaper` method to the `usedRolls` `ArrayList`

Part (c) **getPaperUsed** **4 points**

- +1 Accesses the amount of paper remaining for all elements of the `usedRolls` `ArrayList`; no bounds errors, no missed elements
- +1 Accesses all elements of the `machines` array; no bounds errors, no missed elements
- +1 Accesses the amount of paper remaining on a `Machine` object's `PaperRoll`
- +1 Correctly computes and returns total paper used

4. Hex Grid

- (a) **General Problem:** Write the `getGamePieceCount` method that counts how many `GamePiece` objects are located on the grid.

Refined Problem: Traverse the 2D array of `GamePiece` objects and count the number of cells that are not null.

Algorithm:

- Create a variable to hold the count.
- Traverse the 2D array of values using nested loops.
 - Inside the loops, evaluate each cell of the grid to see if it is null. When we find an element that is not null, increment the count variable.
- Once the entire array has been traversed, the value of the count variable is returned.

Java Code:

```
public int getGamePieceCount()
{
    int count = 0;
    for (int row = 0; row < grid.length; row++)
        for (int col = 0; col < grid[row].length; col++)
            if (grid[row][col] != null)
                count++;
    return count;
}
```

Common Errors:

- Remember that the number of rows is `grid.length` and the number of columns is `grid[row].length` or, since all columns are the same length, `grid[0].length`.
- The return statement has to be outside both loops.

Java Code Alternate Solution:

You can use `for-each` loops to traverse a 2D array.

```

public int getGamePieceCount()
{
    int count = 0;
    for (GamePiece[] row : grid)
        for (GamePiece g : row)
            if (g != null)
                count++;
    return count;
}

```

- (b) **General Problem:** Write the `isAbove` method that returns the `GamePiece` objects that are above an object at a given location on the grid.

Refined Problem: Create an `ArrayList` of `GamePiece` objects that are above the position passed in the parameter, where “above” is defined as having the same column number and a lower row number than another object. If there is no object at the location passed in, null is returned. If there are no objects above the parameter location, an empty `ArrayList` is returned.

Algorithm:

- Determine whether there is a `GamePiece` object at the location specified. If there is not, return null.
- Create an `ArrayList` to hold the `GamePiece` objects to be returned.
- Look in the specified column and the rows from 0 up to the specified row. If any of those cells contain `GamePiece` objects, add them to the `ArrayList`.
- Return the `ArrayList`.

Java Code:

```

public ArrayList<GamePiece> isAbove(int row, int col)
{
    if (grid[row][col] == null)
        return null;
    ArrayList<GamePiece> above = new ArrayList<GamePiece>();
    for (int r = 0; r < row; r++)
        if (grid[r][col] != null)
            above.add(grid[r][col]);
    return above;
}

```

Common Errors:

- Do not count the object itself. That means the loop must stop at $r < \text{row}$, not $r \leq \text{row}$.
- (c) **General Problem:** Write the `addRandom` method that adds a specified number of `GamePiece` objects to the grid in random locations.

Refined Problem: Check to see if there are enough blank cells to add the requested objects. If there are, use a random number generator to generate a row and column number. If the cell at that location is empty, add the object; otherwise, generate a new number. Repeat until all objects have been added.

Algorithm:

- Determine whether there are enough empty cells to hold the requested number of objects.
 - If there are not, return false.
- Loop until all objects have been added.
 - Generate a random int between 0 and number of rows.
 - Generate a random int between 0 and number of columns.
 - Check to see if that cell is free. If it is, add object and decrease number to be added by 1.
- Return true.

Note that this algorithm may take a very long time to run if the grid is large and mostly full. If that is the case, a more efficient

algorithm is to put all available open spaces into a list and then choose a random element from that list.

Java Code:

```
public boolean addRandom(int number)
{
    if (getGamePieceCount() + number > grid.length * grid[0].length)
        return false;
    while (number > 0)
    {
        int row = (int)(Math.random() * grid.length);
        int col = (int)(Math.random() * grid[0].length);
        if (grid[row][col] == null)
        {
            grid[row][col] = new GamePiece();
            number--;
        }
    }
    return true;
}
```

Scoring Guidelines: Hex Grid

Part (a)	getGamePieceCount	2 points
+1	Compares every element to null; no bounds errors, no missed elements	
+1	Returns the correct count	
Part (b)	isAbove	3 points
+1	Returns null if the specified location is null	
+1	Compares to null all elements in the given column with a row number from 0 up to but not including the given row number; no bounds errors, no missed elements	
+1	Creates and returns <code>ArrayList</code> of all elements “above” the given location	
Part (c)	addRandom	4 points
+1	Returns false if there is not sufficient room to add requested elements; must use <code>getGamePieceCount</code> ; returns true after requested number of elements have been added	
+1	Generates a random location; no bounds errors, no missed elements	
+1	Adds the element only if the generated location is null; continues to generate locations in the context of a loop until an element is successfully added (a non-null location is found)	
+1	Continues to add elements in the context of a loop until requested number of elements has been added	

Scoring Worksheet

This worksheet will help you to approximate your performance on Practice Exam 2 in terms of an AP score of 1–5.

Part I (Multiple Choice)

Number right (out of 40 questions) = _____

Part II (Short Answer)

See the scoring guidelines included with the explanations for each of the questions and award yourself points based on those guidelines.

Question 1: Points Obtained (out of 9 possible) _____

Question 2: Points Obtained (out of 9 possible) _____

Question 3: Points Obtained (out of 9 possible) _____

Question 4: Points Obtained (out of 9 possible) _____

Add the points and multiply by 1.1111 _____ $\times$ 1.1111 = _____

Add your totals from both parts of the test
(round to nearest whole number) Total Raw Score _____

Approximate conversion from raw score to AP score

Raw Score Range	AP Score	Interpretation
62–80	5	Extremely Well Qualified
44–61	4	Well Qualified
31–43	3	Qualified
25–30	2	Possibly Qualified
0–24	1	No Recommendation